Counting and Cardinality	Operations & Algebraic Thinking	Number & Operations in Base Ten	Measurement & Data	Geometry	
K.CC	K.OA	K.NBT	PK.MD	PK.G	
 Know number names and the count sequence. 1. Count to 100 by ones and by tens. 2. Count forward beginning from a given number within the known sequence (instead of having to begin at 1). 3. Write numbers from 0 to 20. Represent a number of objects with a written numeral 0-20 (with 0 representing a count of no objects). Count to tell the number of objects. 	 Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from. 1. Represent addition and subtraction with objects, fingers, mental images, drawings¹, sounds (e.g., claps), acting out situations, verbal explanations, expressions, or equations. 2. Solve addition and subtraction word 	 Work with numbers 11-19 to gain foundations for place value. 1. Compose and decompose numbers from 11 to 19 into ten ones and some further ones, e.g., by using objects or drawings, and record each composition or decomposition by a drawing or equation (such as 18 = 10 + 8); understand that these numbers are composed of ten ones and one, two, three, four, five, six, seven, eight, or pipe ones. 	 Describe and compare measurable attributes. 1. Describe measurable attributes of objects, such as length or weight. Describe several measurable attributes of a single object. 2. Directly compare two objects with a measurable attribute in common, to see which object has "more of"/"less of" the attribute, and describe the difference. For example, directly compare the heights of two children and 	Identify and describe shapes (squares, circles, triangles, rectangles, hexagons, cubes, cones, cylinders, and spheres).1. Describe objects in the environment using names of shapes, and describe the relative positions of these objects using terms such as above, below, beside, in front of, behind, and next to.2. Correctly name shapes regardless of their	
 4. Understand the relationship between numbers and quantities; connect counting to cardinality. a. When counting objects, say the number names in the standard order, pairing each object with one and only one number name and each number name with one and only one object. b. Understand that the last number name said tells the number of objects counted. The number of objects is the same regardless of their arrangement or the order in which they were counted. c. Understand that each successive number name refers to a quantity that is one larger. Develop understanding of ordinal numbers (first through tenth) to describe the relative position and magnitude of whole numbers. 5. Count to answer "how many?" questions about as many as 20 things arranged in a line, a rectangular array, or a circle, or as many as 10 things in a scattered configuration; given a number from 1–20, count out that many objects. Compare numbers. 6. Identify whether the number of objects in one group is greater than, less than, or equal to the number of objects in another group, e.g., by using matching and counting strategies.¹ 7. Compare two numbers between 1 and 10 presented as written numerals. ¹ Include groups with up to ten objects. 	 Solve addition and subtraction word problems, and add and subtract within 10, e.g., by using objects or drawings to represent the problem. Decompose numbers less than or equal to 10 into pairs in more than one way, e.g., by using objects or drawings, and record each decomposition by a drawing or equation (e.g., 5 = 2 + 3 and 5 = 4 + 1). For any number from 1 to 9, find the number that makes 10 when added to the given number, e.g., by using objects or drawings, and record the answer with a drawing or equation. Fluently add and subtract within 5. ¹ Drawings need not show details, but should show the mathematics in the problem. (This applies wherever drawings are mentioned in the Standards.) 	nine ones.	Compare the neights of two children and describe one child as taller/shorter. Classify objects and count the number of objects in each category. 3. Classify objects into given categories; count the numbers of objects in each category and sort the categories by count. ¹ ¹ Limit category counts to be less than or equal to 10.	 Correctly name snapes regardless of their orientations or overall size. Identify shapes as two-dimensional (lying in a plane, "flat") or three-dimensional ("solid"). Analyze, compare, create, and compose shapes. Analyze and compare two- and three-dimensional shapes, in different sizes and orientations, using informal language to describe their similarities, differences, parts (e.g., number of sides and vertices/"corners") and other attributes (e.g., having sides of equal length). Model shapes in the world by building shapes from components (e.g., sticks and clay balls) and drawing shapes. Compose simple shapes to form larger shapes. For example, "Can you join these two triangles with full sides touching to make a rectangle?" 	

Mathematics Common Core Learning Standards—Grades K-5

Operations & Algebraic Thinking 1.OA	making ten (e.g., $8 + 6 = 8 + 2 + 4 = 10 + 4 = 14$); decomposing a number leading to a ten (e.g., $13 - 4 = 13 - 3 - 1 = 10 - 1 = 9$); using the	Number & Operations in Base Ten 1.NBT Extend the counting sequence.	Measurement & Data 1.MD	Geometry 1.G
Represent and solve problems involving addition and subtraction. 1. Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem. ¹ 2. Solve word problems that call for addition of three whole numbers whose sum is less than or equal to 20, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem. Understand and apply properties of operations and the relationship between addition and subtraction. 3. Apply properties of operations as strategies to add and subtract. ² Examples: If $8 + 3 = 11$ is known, then $3 + 8 = 11$ is also known. (Commutative property of addition.) To add $2 + 6$ + 4, the second two numbers can be added to make a ten, so $2 + 6 + 4 = 2 + 10 = 12$. (Associative property of addition.) 4. Understand subtraction as an unknown- addend problem. For example, subtract $10 - 8$ by finding the number that makes 10 when added to 8. Add and subtract within 20. 5. Relate counting to addition and subtraction (e.g., by counting on 2 to add 2). 6. Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as counting on;	(e.g., howing that $8 + 4 = 12$, one knows $12 - 8 = 4$); and creating equivalent but easier or known sums (e.g., adding $6 + 7$ by creating the known equivalent $6 + 6 + 1 = 12 + 1 = 13$). Work with addition and subtraction equations. 7. Understand the meaning of the equal sign, and determine if equations involving addition and subtraction are true or false. For example, which of the following equations are true and which are false? $6 = 6$, $7 = 8 - 1$, $5 + 2 = 2 + 5$, $4 + 1 = 5 + 2$. 8. Determine the unknown whole number in an addition or subtraction equation relating three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations $8 + ? = 11$, $5 = -3$, $6 + 6 = -2$. 1 See Glossary, Table 1. 2 Students need not use formal terms for these properties.	 Count to 120, starting at any number less than 120. In this range, read and write numerals and represent a number of objects with a written numeral. Understand place value. Understand that the two digits of a two-digit number represent amounts of tens and ones. Understand the following as special cases: a. 10 can be thought of as a bundle of ten ones — called a "ten." b. The numbers from 11 to 19 are composed of a ten and one, two, three, four, five, six, seven, eight, or nine ones. c. The numbers 10, 20, 30, 40, 50, 60, 70, 80, 90 refer to one, two, three, four, five, six, seven, eight, or nine tens (and 0 ones). Compare two two-digit numbers based on meanings of the tens and ones digits, recording the results of comparisons with the symbols >, =, and <. Use place value understanding and properties of operations to add /subtract. Add within 100, including adding a two-digit number and a one-digit number, and adding a two-digit number and a one-digit number, and adding a two-digit number and a multiple of 10, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used. Understand that in adding two-digit numbers, one adds tens and tens, ones and ones; and sometimes it is necessary to compose a ten. Given a two-digit number, without having to count; explain the reasoning used. Subtract multiples of 10 in the range 10-90 from multipl	 Measure lengths indirectly and by iterating length units. 1. Order three objects by length; compare the lengths of two objects indirectly by using a third object. 2. Express the length of an object as a whole number of length units, by laying multiple copies of a shorter object (the length unit) end to end; understand that the length measurement of an object is the number of same-size length units that span it with no gaps or overlaps. <i>Limit to contexts where the object being measured is spanned by a whole number of length units with no gaps or overlaps.</i> Tell and write time and money. 3. Tell and write time in hours and half-hours using analog and digital clocks. Recognize and identify coins, their names, and their value. Represent and interpret data. 4. Organize, represent, and interpret data with up to three categories; ask and answer questions about the total number of data points, how many in each category, and how many more or less are in one category than in another. 	Reason with shapes and their attributes. 1. Distinguish between defining attributes (e.g., triangles are closed and three-sided) versus non- defining attributes (e.g., color, orientation, overall size) ; build and draw shapes to possess defining attributes. 2. Compose two-dimensional shapes (rectangles, squares, trapezoids, triangles, half-circles, and quarter-circles) or three-dimensional shapes (cubes, right rectangular prisms, right circular cones, and right circular cylinders) to create a composite shape, and compose new shapes from the composite shape. ¹ 3. Partition circles and rectangles into two and four equal shares, describe the shares using the words <i>halves, fourths</i> , and <i>quarter of</i> . Describe the whole as two of, or four of the shares. Understand for these examples that decomposing into more equal shares creates smaller shares. ¹ Students do not need to learn formal names such as "right rectangular prism."

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Operations & Algebraic Thinking	Number & Operations in Base Ten	Measurement & Data	Geometry
2.0A	2.NBT	2.MD	2.G
Represent and solve problems involving addition and subtraction.	Understand place value. 1. Understand that the three digits of a three-digit number represent	Measure and estimate lengths in standard units. 1. Measure the length of an object by selecting and using	Reason with shapes and their attributes. 1. Recognize and draw shapes having specified attributes,
1. Use addition and subtraction within 100 to solve one-	amounts of hundreds, tens, and ones; e.g., 706 equals 7 hundreds, 0	appropriate tools such as rulers, yardsticks, meter sticks, and	such as a given number of angles or a given number of equal
	tens, and 6 ones. Understand the following as special cases:	measuring tapes.	faces. ¹ Identify triangles, quadrilaterals, pentagons, hexagons,
and two-step word problems involving situations of	a. 100 can be thought of as a bundle of ten tens — called a	2. Measure the length of an object twice, using length units of	and cubes.
adding to, taking from, putting together, taking apart,	"hundred." b. The numbers 100, 200, 300, 400, 500, 600, 700, 800, 900	different lengths for the two measurements; describe how the	
and comparing, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the	refer to one, two, three, four, five, six, seven, eight, or nine	two measurements relate to the size of the unit chosen.	2. Partition a rectangle into rows and columns of same-size
unknown number to represent the problem. ¹	hundreds (and 0 tens and 0 ones).	3. Estimate lengths using units of inches, feet, centimeters,	squares and count to find the total number of them.
unknown number to represent the problem.		and meters.	2. Destition simples and restancies into two three sufering equal
Add and subtract within 20.	2. Count within 1000; skip-count by 5s, 10s, and 100s.	4. Measure to determine how much longer one object is than another, expressing the length difference in terms of a	3. Partition circles and rectangles into two, three, or four equal shares, describe the shares using the words halves, thirds,
2. Fluently add and subtract within 20 using mental	3. Read and write numbers to 1000 using base-ten numerals,	standard length unit.	half of, a third of, etc., and describe the whole as two halves,
strategies. ² By end of Grade 2, know from memory all	number names, and expanded form.		three thirds, four fourths. Recognize that equal shares of
sums of two one-digit numbers.		Relate addition and subtraction to length.	identical wholes need not have the same shape.
	4. Compare two three-digit numbers based on meanings of the hundreds, tens, and ones digits, using >, =, and < symbols to record	5. Use addition and subtraction within 100 to solve word	
Work with equal groups of objects to gain	the results of comparisons.	problems involving lengths that are given in the same units,	
foundations for multiplication.		e.g., by using drawings (such as drawings of rulers) and	¹ Sizes are compared directly or visually, not compared by
3. Determine whether a group of objects (up to 20) has	Use place value understanding and properties of	equations with a symbol for the unknown number to represent the problem.	measuring.
an odd or even number of members, e.g., by pairing	operations to add and subtract. 5. Fluently add and subtract within 100 using strategies based on	6. Represent whole numbers as lengths from 0 on a number	
objects or counting them by 2s; write an equation to	place value, properties of operations, and/or the relationship between	line diagram with equally spaced points corresponding to the	
express an even number as a sum of two equal	addition and subtraction.	numbers 0, 1, 2,, and represent whole-number sums and	
addends.		differences within 100 on a number line diagram.	
	 Add up to four two-digit numbers using strategies based on place value and properties of operations. 		
4. Use addition to find the total number of objects		Work with time and money.	
arranged in rectangular arrays with up to 5 rows and up	7. Add and subtract within 1000, using concrete models or drawings	7. Tell and write time from analog and digital clocks to the	
to 5 columns; write an equation to express the total as a	and strategies based on place value, properties of operations, and/or	nearest five minutes, using a.m. and p.m. 8. Solve word problems involving dollar bills, quarters, dimes,	
sum of equal addends.	the relationship between addition and subtraction; relate the strategy to a written method. Understand that in adding or subtracting three-	nickels, and pennies, using $\$ and ϕ symbols appropriately.	
	digit numbers, one adds or subtracts hundreds and hundreds, tens	Example: If you have 2 dimes and 3 pennies, how many cents	
	and tens, ones and ones; and sometimes it is necessary to compose	do you have?	
¹ See Glossary, Table 1.	or decompose tens or hundreds.		
² See standard 1.OA.6 for a list of mental strategies.	8. Mentally add 10 or 100 to a given number 100–900, and mentally	Represent and interpret data.	
	subtract 10 or 100 from a given number 100–900.	9. Generate measurement data by measuring lengths of	
		several objects to the nearest whole unit, or by making repeated measurements of the same object. Show the	
	9. Explain why addition and subtraction strategies work, using place	measurements by making a line plot, where the horizontal	
	value and the properties of operations. ¹	scale is marked off in whole-number units.	
		10. Draw a picture graph and a bar graph (with single-unit	
	¹ Explanations may be supported by drawings or objects.	scale) to represent a data set with up to four categories. Solve	
		simple put-together, take-apart, and compare problems ¹ using	
		information presented in a bar graph.	
		¹ See Glossary, Table 1.	

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Operations & Algebraic Thinking	Number & Operations in Base Ten	Number & Operations - Fractions	Measurement & Data	Geometry
3.OA	3.NBT	3.NF	3.MD	3.G
			-	
Represent and solve problems involving multiplication	Use place value understanding and	Develop understanding of fractions as numbers.	Solve problems involving measurement and estimation of intervals of time, liquid volumes, and masses of objects.	Reason with shapes and their attributes.
and division. 1. Interpret products of whole numbers, e.g., interpret 5 × 7 as the	properties of operations to perform multi-	1. Understand a fraction 1/b as the quantity formed	1. Tell and write time to the nearest minute and measure time intervals	1. Understand that shapes in different categories
total number of objects in 5 groups of 7 objects each. For example,	digit arithmetic. ¹	by 1 part when a whole is partitioned into b equal	in minutes. Solve word problems involving addition and subtraction of	(e.g., rhombuses, rectangles, and others) may
describe a context in which a total number of objects can be	1. Use place value understanding to round whole	parts; understand a fraction a/b as the quantity	time intervals in minutes, e.g., by representing the problem on a	share attributes (e.g., having four sides), and that
expressed as 5 × 7.		formed by a parts of size 1/b.	number line diagram.	
2. Interpret whole-number quotients of whole numbers, e.g., interpret	numbers to the nearest 10 or 100.		 Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l).¹ Add, 	the shared attributes can define a larger category
$56 \div 8$ as the number of objects in each share when 56 objects are		2. Understand a fraction as a number on the number	subtract, multiply, or divide to solve one-step word problems involving	(e.g., quadrilaterals). Recognize rhombuses,
partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each. For	2. Fluently add and subtract within 1000 using	line; represent fractions on a number line diagram.	masses or volumes that are given in the same units, e.g., by using	rectangles, and squares as examples of
example, describe a context in which a number of shares or a number	strategies and algorithms based on place value,	a. Represent a fraction 1/b on a number line	drawings (such as a beaker with a measurement scale) to represent	quadrilaterals, and draw examples of
of groups can be expressed as 56 ÷ 8.	properties of operations, and/or the relationship	diagram by defining the interval from 0 to 1	the problem. ²	quadrilaterals that do not belong to any of these
3. Use multiplication and division within 100 to solve word problems in	between addition and subtraction.	as the whole and partitioning it into b equal	Represent and interpret data.	
situations involving equal groups, arrays, and measurement	between addition and subtraction.		3. Draw a scaled picture graph and a scaled bar graph to represent a	subcategories.
quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem. ¹		parts. Recognize that each part has size	data set with several categories. Solve one- and two-step "how many	2. Partition shapes into parts with equal areas.
4. Determine the unknown whole number in a multiplication or division	3. Multiply one-digit whole numbers by multiples	1/b and that the endpoint of the part based	more" and "how many less" problems using information presented in	Express the area of each part as a unit fraction
equation relating three whole numbers. For example, determine the	of 10 in the range 10–90 (e.g., 9 × 80, 5 × 60)	at 0 locates the number 1/b on the number	scaled bar graphs. For example, draw a bar graph in which each	of the whole. For example, partition a shape into
unknown number that makes the equation true in each of the	using strategies based on place value and	line.	square in the bar graph might represent 5 pets.	4 parts with equal area, and describe the area of
equations 8 × ? = 48, 5 = _ ÷ 3, 6 × 6 = ?	properties of operations.	b. Represent a fraction <i>a/b</i> on a number line	 Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a 	each part as 1/4 of the area of the shape.
Understand properties of multiplication and the	properties of operations.	diagram by marking off a lengths 1/b from	line plot, where the horizontal scale is marked off in appropriate	each part as 1/4 of the area of the shape.
relationship between multiplication and division.		Recognize that the resulting interval has	units- whole numbers, halves, or quarters.	
5. Apply properties of operations as strategies to multiply and divide. ²		size a/b and that its endpoint locates the		
Examples: If $6 \times 4 = 24$ is known, then $4 \times 6 = 24$ is also known.	¹ A range of algorithms may be used.	number <i>alb</i> on the number line.	Geometric measurement: understand concepts of area and relate	
(Commutative property of multiplication.) 3 × 5 × 2 can be found by 3		3. Explain equivalence of fractions in special cases,	area to multiplication and to addition. 5. Recognize area as an attribute of plane figures and understand	
$x = 5 = 15$, then $15 \times 2 = 30$, or by $5 \times 2 = 10$, then $3 \times 10 = 30$.		and compare fractions by reasoning about their size.	concepts of area measurement.	
(Associative property of multiplication.) Knowing that $8 \times 5 = 40$ and $8 \times 2 = 16$, one can find 8×7 as $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16$		a. Understand two fractions as equivalent	a. A square with side length 1 unit, called "a unit square,"	
2 - 10, one can ind $3 - 1 as 3 - (3 + 2) - (3 - 3) + (3 - 2) - 40 + 10= 56. (Distributive property.)$		(equal) if they are the same size, or the	is said to have "one square unit" of area, and can be	
6. Understand division as an unknown-factor problem. For example,			used to measure area.	
find 32 ÷ 8 by finding the number that makes 32 when multiplied by 8.		same point on a number line.	b. A plane figure which can be covered without gaps or overlaps by n unit squares is said to have an area of n	
		b. Recognize and generate simple equivalent	square units.	
Multiply and divide within 100.		fractions, e.g., 1/2 = 2/4, 4/6 = 2/3). Explain	6. Measure areas by counting unit squares (square cm, square m,	
7. Fluenty multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that 8 ×		why the fractions are equivalent, e.g., by	square in, square ft, and improvised units).	
$5 = 40$, one knows $40 \div 5 = 8$) or properties of operations. By the end		using a visual fraction model.	7. Relate area to the operations of multiplication and addition.	
of Grade 3, know from memory all products of two one-digit numbers.		 Express whole numbers as fractions, and 	 Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same 	
		recognize fractions that are equivalent to	as would be found by multiplying the side lengths.	
Solve problems involving the four operations, and		whole numbers. Examples: Express 3 in	b. Multiply side lengths to find areas of rectangles with	
identify and explain patterns in arithmetic.		the form $3 = 3/1$; recognize that $6/1 = 6$;	whole-number side lengths in the context of solving real	
8. Solve two-step word problems using the four operations. Represent		locate 4/4 and 1 at the same point of a	world and mathematical problems, and represent whole-	
these problems using equations with a letter standing for the unknown		number line diagram.	number products as rectangular areas in mathematical reasoning.	
quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. ³		d. Compare two fractions with the same	c. Use tiling to show in a concrete case that the area of a	
 Identify arithmetic patterns (including patterns in the addition table 		numerator or the same denominator by	rectangle with whole-number side lengths a and $b + c$ is	
or multiplication table), and explain them using properties of			the sum of $a \times b$ and $a \times c$. Use area models to	
operations. For example, observe that 4 times a number is always		reasoning about their size. Recognize that	represent the distributive property in mathematical	
even, and explain why 4 times a number can be decomposed into two		comparisons are valid only when the two	reasoning. d. Recognize area as additive. Find areas of rectilinear	
equal addends.		fractions refer to the same whole. Record	figures by decomposing them into non-overlapping	
		the results of comparisons with the symbols	rectangles and adding the areas of the non-overlapping	
¹ See Glossary, Table 2.		>, =, or <, and justify the conclusions, e.g.,	parts, applying this technique to solve real world	
² Students need not use formal terms for these properties.		by using a visual fraction model.	problems.	
³ This standard is limited to problems posed with whole numbers and			Geometric measurement: recognize perimeter as an attribute of plane figures and distinguish between linear and area measures.	
having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to			8. Solve real world and mathematical problems involving perimeters of	¹ Excludes compound units such as cm3 and finding the geometric volume of a container.
specify a particular order.		¹ Grade 3 expectations in this domain are limited to	polygons, including finding the perimeter given the side lengths,	² Excludes multiplicative comparison problems (problems involving
-r 7 Sharana		fractions with denominators 2, 3, 4, 6, 8.	finding an unknown side length, and exhibiting rectangles with the	notions of "times as much"; see Glossary, Table 2).
			same perimeter and different areas or with the same area and	
			different perimeters.	

Operations & Algebraic Thinking	Number & Operations in Base Ten	Number & Operations - Fractions	Measurement & Data	Geometry
	4.NBT	4.NF	4.MD	4.G
Use the four operations with whole numbers to solve problems.	Generalize place value understanding for multi- digit whole numbers.	Extend understanding of fraction equivalence and ordering.	Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.	Draw and identify lines and angles, and classify shapes by properties of their lines and angles.
1. Interpret a multiplication equation as a comparison,	1. Recognize that in a multi-digit whole number, a digit	1. Explain why a fraction a/b is equivalent to a fraction (n × a)/(n × b) by using	1. Know relative sizes of measurement units within one	1. Draw points, lines, line segments, rays, angles
e.g., interpret $35 = 5 \times 7$ as a statement that 35 is 5	in one place represents ten times what it represents in	visual fraction models, with attention to how the number and size of the parts differ even though the two fractions themselves are the same size. Use this	system of units including km, m, cm; kg, g; lb, oz.; l, ml; hr,	(right, acute, obtuse), and perpendicular and parallel
times as many as 7 and 7 times as many as 5.	the place to its right. For example, recognize that 700	principle to recognize and generate equivalent fractions.	min, sec. Within a single system of measurement, express	lines. Identify these in two-dimensional figures.
Represent verbal statements of multiplicative	\div 70 = 10 by applying concepts of place value and	 Compare two fractions with different numerators and different denominators, e.g., by creating common denominators or numerators, or by comparing to a 	measurements in a larger unit in terms of a smaller unit.	
comparisons as multiplication equations.	division.	benchmark fraction such as 1/2. Recognize that comparisons are valid only when	Record measurement equivalents in a two-column table. For example, know that 1 ft is 12 times as long as 1 in. Express	2. Classify two-dimensional figures based on the
compansons as multiplication equations.		the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions, e.g., by using a visual fraction	the length of a 4 ft snake as 48 in. Generate a conversion	presence or absence of parallel or perpendicular lines,
2. Multiply or divide to solve word problems involving	2. Read and write multi-digit whole numbers using	model.	table for feet and inches listing the number pairs (1, 12), (2,	or the presence or absence of angles of a specified
multiplicative comparison, e.g., by using drawings and	base-ten numerals, number names, and expanded	Build fractions from unit fractions by applying and	24), (3, 36),	size. Recognize right triangles as a category, and
equations with a symbol for the unknown number to	form. Compare two multi-digit numbers based on	extending previous understandings of operations on	2. Use the four operations to solve word problems involving	identify right triangles.
represent the problem, distinguishing multiplicative	meanings of the digits in each place, using >, =, and <	whole numbers.	distances, intervals of time, liquid volumes, masses of	
comparison from additive comparison. ¹	symbols to record the results of comparisons.	 Understand a fraction <i>a/b</i> with <i>a</i> > 1 as a sum of fractions 1/<i>b</i>. Understand addition and subtraction of fractions as joining and 	objects, and money, including problems involving simple	3. Recognize a line of symmetry for a two-dimensional
,	,	separating parts referring to the same whole.	fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller	figure as a line across the figure such that the figure
3. Solve multistep word problems posed with whole	3. Use place value understanding to round multi-digit	Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each	unit. Represent measurement quantities using diagrams such	can be folded along the line into matching parts.
numbers and having whole-number answers using the	whole numbers to any place.	decomposition by an equation. Justify decompositions, e.g., by	as number line diagrams that feature a measurement scale.	Identify line-symmetric figures and draw lines of
four operations, including problems in which		using a visual fraction model. <i>Examples</i> : 3/8 = 1/8 + 1/8 + 1/8 ; 3/8 = 1/8 + 2/8 ; 2 1/8 = 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8.	3. Apply the area and perimeter formulas for rectangles in	symmetry.
remainders must be interpreted. Represent these	Use place value understanding and properties of	c. Add and subtract mixed numbers with like denominators, e.g., by	real world and mathematical problems. For example, find the	
problems using equations with a letter standing for the	operations to perform multi-digit arithmetic.	replacing each mixed number with an equivalent fraction, and/or by using properties of operations and the relationship between	width of a rectangular room given the area of the flooring and	
unknown quantity. Assess the reasonableness of	4. Fluently add and subtract multi-digit whole numbers	addition and subtraction.	the length, by viewing the area formula as a multiplication equation with an unknown factor.	
answers using mental computation and estimation	using the standard algorithm.	 Solve word problems involving addition and subtraction of fractions referring to the same whole and having like 	equation with an unknown lactor.	
strategies including rounding.		denominators, e.g., by using visual fraction models and equations	Represent and interpret data.	
	5. Multiply a whole number of up to four digits by a	to represent the problem. 4. Apply and extend previous understandings of multiplication to multiply a fraction	4. Make a line plot to display a data set of measurements in	
Gain familiarity with factors and multiples.	one-digit whole number, and multiply two two-digit	by a whole number. a. Understand a fraction <i>a/b</i> as a multiple of 1/ <i>b</i> . For example, use a	fractions of a unit (1/2, 1/4, 1/8). Solve problems involving	
4. Find all factor pairs for a whole number in the range	numbers, using strategies based on place value and	visual fraction model to represent 5/4 as the product $5 \times (1/4)$,	addition and subtraction of fractions by using information	
1–100. Recognize that a whole number is a multiple of	the properties of operations. Illustrate and explain the	recording the conclusion by the equation $5/4 = 5 \times (1/4)$. b. Understand a multiple of a/b as a multiple of $1/b$, and use this	presented in line plots. For example, from a line plot find and	
each of its factors. Determine whether a given whole	calculation by using equations, rectangular arrays,	understanding to multiply a fraction by a whole number. For	interpret the difference in length between the longest and shortest specimens in an insect collection.	
number in the range 1–100 is a multiple of a given	and/or area models.	example, use a visual fraction model to express $3 \times (2/5)$ as $6 \times (1/5)$, recognizing this product as $6/5$. (In general, $n \times (a/b) = (n \times a)$		
one-digit number. Determine whether a given whole		a)/b.)	Geometric measurement: understand concepts of angle	
number in the range 1–100 is prime or composite.	6. Find whole-number quotients and remainders with	c. Solve word problems involving multiplication of a fraction by a	and measure angles.	
	up to four-digit dividends and one-digit divisors, using	whole number, e.g., by using visual fraction models and	5. Recognize angles as geometric shapes that are formed	
	strategies based on place value, the properties of	equations to represent the problem. For example, if each person at a party will eat 3/8 of a pound of roast beef, and there will be 5	wherever two rays share a common endpoint, and	
Generate and analyze patterns.	operations, and/or the relationship between	people at the party, how many pounds of roast beef will be	understand concepts of angle measurement: a. An angle is measured with reference to a circle	
5. Generate a number or shape pattern that follows a	multiplication and division. Illustrate and explain the	needed? Between what two whole numbers does your answer lie?	with its center at the common endpoint of the	
given rule. Identify apparent features of the pattern	calculation by using equations, rectangular arrays,	Understand desired notation for functions, and a surround	rays, by considering the fraction of the circular	
that were not explicit in the rule itself. For example, given the rule "Add 3" and the starting number 1,	and/or area models.	Understand decimal notation for fractions, and compare decimal fractions.	arc between the points where the two rays	
с ,		5. Express a fraction with denominator 10 as an equivalent fraction with	intersect the circle. An angle that turns through	
generate terms in the resulting sequence and observe that the terms appear to alternate between odd and	¹ Grade 4 expectations in this domain are limited to	denominator 100, and use this technique to add two fractions with respective denominators 10 and 100. ² For example, express 3/10 as 30/100, and add 3/10 +	1/360 of a circle is called a "one-degree angle,"	
even numbers. Explain informally why the numbers	whole numbers less than or equal to 1.000.000	4/100 = 34/100.	and can be used to measure angles. b. An angle that turns through <i>n</i> one-degree angles	
will continue to alternate in this way.		 Use decimal notation for fractions with denominators 10 or 100. For example, rewrite 0.62 as 62/100; describe a length as 0.62 meters; locate 0.62 on a number 	is said to have an angle measure of <i>n</i> degrees.	
win continuo to anomato in tino way.		line diagram.	6. Measure angles in whole-number degrees using a	
		Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole.	protractor. Sketch angles of specified measure.	
¹ See Glossary, Table 2.		Record the results of comparisons with the symbols >, =, or <, and justify the	7. Recognize angle measure as additive. When an angle is	
		conclusions, e.g., by using a visual model.	decomposed into non-overlapping parts, the angle measure	
		¹ Grade 4 expectations in this domain are limited to fractions with denominators 2,	of the whole is the sum of the angle measures of the parts.	
		3, 4, 5, 6, 8, 10, 12, 100. ² Students who can generate equivalent fractions can develop strategies for	Solve addition and subtraction problems to find unknown angles on a diagram in real world and mathematical	
		adding fractions with unlike denominators in general. But addition and subtraction	problems, e.g., by using an equation with a symbol for the	
		with unlike denominators in general is not a requirement at this grade.	unknown angle measure.	

Operations & Algebraic Thinking	Number & Operations in Base Ten	Number & Operations - Fractions	Measurement & Data	Geometry
5.OA	5.NBT	5.NF	5.MD	5.G
 Write and interpret numerical expressions 1. Use parentheses, brackets, or braces in numerical expressions, and evaluate expressions with these symbols. 2. Write simple expressions that record calculations with numbers, and interpret numerical expressions with utevaluating them. For example, express the calculation "add 8 and 7, then multiply by 2" as 2 × (8 + 7). Recognize that 3 × (18932 + 921) is three times as large as 18932 + 921, without having to calculate the indicated sum or product. Analyze patterns and relationships. 3. Generate two numerical patterns using two given rules. Identify apparent relationships between corresponding terms. Form ordered pairs consisting of corresponding terms from the two patterns, and graph the ordered pairs on a coordinate plane. For example, given the rule "Add 3" and the starting number 0, generate terms in the resulting sequences, and observe that the terms in one sequence are twice the corresponding terms in the other sequence. Explain informally why this is so. 	 Understand the place value system. 1. Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left. 2. Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10. 3. Read, write, and compare decimals to thousandths. a. Read and write decimals to thousandths. a. Read and write decimals to thousandths. a. Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, e.g., 347.392 = 3 × 100 + 4 × 10 + 7 × 1 + 3 × (1/10) + 9 × (1/100) + 2 × (1/1000). b. Compare two decimals to thousandths based on meanings of the digits in each place, using >, =, and < symbols to record the results of comparisons. 4. Use place value understanding to round decimals to any place. Perform operations with multi-digit whole numbers and with decimals to hundredths. 5. Fluently multiply multi-digit whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and divison. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models. 7. Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used. 	 Use equivalent fractions as a strategy to add and subtract fractions. 1. Add and subtract fractions with unlike denominators (including mixed numbers) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators. For example, 20 + 5/4 = 8/12 + 15/12 = 23/12. (In general, ab + c/d = (al + c/b/d.) 2. Solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators, e.g., by using visual fraction models or equations to represent the problem. Use benchmark fractions and number sense of fractions to estimate mentally and assess the reasonableness of answers. For example, recognize an incorrect result 2/5 + 1/2 = 3/7, by observing that 3/7 < 1/2. Apply and extend previous understandings of multiplication and division to multiply and divide fractions. 3. Interpret a fractions a division of whole numbers leading to answers in the form of fractions or mixed numbers, e.g., by using visual fraction models or equations to represent the problem. For example, interpret 3/4 as the result of dividing 3 by 4, noting that 3/4 multiplied by 4 equals 3, and that when 3 wholes are stared equally among 4 people each person has a stare of size 3/4. If 9 people want to share a 50-pound sack of rice equaliby weight, how many pounds of rice should each person gel? Between what two whole numbers does your answer lie? 4. Apply and extend previous understandings of multiplication to multiply affaction rowells are stared equally among 4 people each person the a stare of size 3/4. If 9 people want to share a 50-pound sack of rice equaliby the with (2/3) × (4/5) = 8/15. (In general, (4/b) × (g a) a a parts of a partition of a into be equal parts; equivalently, as the result of a sequence of operations a × 4-b. For example, use a visual fraction model to show (2/3) × 4 = 8/3, and create a story context for th	 Convert like measurement units within a given measurement system. 1. Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05 m), and use these conversions in solving multi-step, real world problems. Represent and interpret data. 2. Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). Use operations on fractions for this grade to solve problems involving information presented in line plots. For example, given different measurements of liquid in identical beakers, find the amount of liquid each beaker would contain if the total amount in all the beakers were redistributed equally. Geometric measurement: understand concepts of volume and relate volume to multiplication and to addition. 3. Recognize volume as an attribute of solid figures and understand concepts of volume measurement. a. A cube with side length 1 unit, called a "unit cube," is said to have "one cubic unit" of volume, and can be used to measure volume. b. A solid figure which can be packed without gaps or overlaps using n unit cubes is said to have a volume of n cubic units. 5. Relate volume to the operations of multiplication and addition and solve real world and mathematical problems involving volume. a. Find the volume of a right rectangular prism with whole-number side lengths by packing it with unit cubes, and show that the volume is the same as would be found by multiplying the edge lengths, equivalently by multiplication. b. Apply the formulas V = I × w × h and V = b × h for rectangular prisms to find volumes of right rectangular prisms with whole-number products as volumes, e.g., to represent the associative property of multiplication. b. Apply the formulas V = I × w × h and V = b × h for rectangular prisms by addity. Find volumes of solid figures composed of two non-overlapping right rectangular prisms by addity the volume of solid	 Graph points on the coordinate plane to solve real-world and mathematical problems. 1. Use a pair of perpendicular number lines, called axes, to define a coordinate system, with the intersection of the lines (the origin) arranged to coincide with the 0 on each line and a given point in the plane located by using an ordered pair of number, called its coordinates. Understand that the first number indicates how far to travel from the origin in the direction of one axis, and the second number indicates how far to travel from the second axis, with the convention that the names of the two axes and the coordinates correspond (e.g., <i>x</i>-axis and <i>x</i>-coordinate, <i>y</i>-axis and <i>y</i>-coordinate). 2. Represent real world and mathematical problems by graphing points in the first quadrant of the coordinate plane, and interpret coordinate values of points in the context of the situation. Classify two-dimensional figures into categories based on their properties. 3. Understand that attributes belonging to a category of two-dimensional figures also belong to all subcategories of that category. For example, all rectangles have four right angles and squares are rectangles, so all squares have four right angles. 4. Classify two-dimensional figures in a hierarchy based on properties.